Cambridge IGCSE™

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MATHEMATICS **0580/22**

Paper 2 (Extended) **February/March 2023**

1 hour 30 minutes

You must answer on the question paper.

You will need: Geometrical instruments

INSTRUCTIONS
- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- You should use a calculator where appropriate.
- You may use tracing paper.
- You must show all necessary working clearly.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- For π, use either your calculator value or 3.142.

INFORMATION
- The total mark for this paper is 70.
- The number of marks for each question or part question is shown in brackets [ ].

This document has **12** pages.

[Turn over

1

| 12 | 15 | 27 | 29 | 91 | 93 |

From the list of numbers, write down

(a) a cube number

.... [1]

(b) a prime number.

.... [1]

2 $\mathbf{v} = \begin{pmatrix} -1 \\ 3 \end{pmatrix}$ $\mathbf{y} = \begin{pmatrix} 2 \\ 5 \end{pmatrix}$
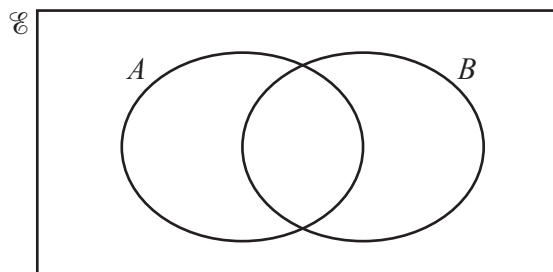
Find

(a) $\mathbf{v} - \mathbf{y}$

$\begin{pmatrix} \\ \end{pmatrix}$ [1]

(b) $2\mathbf{v}$.

$\begin{pmatrix} \\ \end{pmatrix}$ [1]

3

On the Venn diagram, shade the region $A \cap B$.   [1]

4   23,   17,   11,   5, ...

(a) Write down the next number in this sequence.

.... [1]

(b) Find the nth term of this sequence.

.... [2]

5 Factorise completely.
$$8g - 2g^2$$

.... [2]

6 **Without using a calculator**, work out $\dfrac{4}{7} \div 8$.

You must show all your working and give your answer as a fraction in its simplest form.

.... [2]

7 Solve.

(a) $15t + 8 = 4 - t$

$t =$ .... [2]

(b) $\dfrac{25 - 2u}{3} = 2$

$u =$ .... [2]

8 Calculate 0.3^2.
Give your answer in standard form.

.... [2]

9 Solve the simultaneous equations.
You must show all your working.

$$3x - 2y = 19$$
$$x + y = 3$$

$x =$ ....

$y =$ .... [3]

10
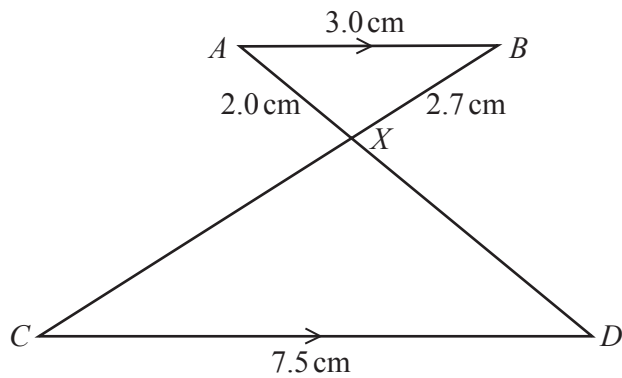
In the diagram, *AB* and *CD* are parallel.
The lines *CB* and *AD* intersect at *X*.
$AB = 3.0$ cm, $AX = 2.0$ cm, $BX = 2.7$ cm and $CD = 7.5$ cm.

Find the length of *BC*.

$BC =$ .... cm [3]

11 Find the highest common factor (HCF) of $12x^{12}$ and $16x^{16}$.

.... [2]

12 In a regular polygon, the interior angle and the exterior angle are in the ratio interior : exterior = 11 : 1.
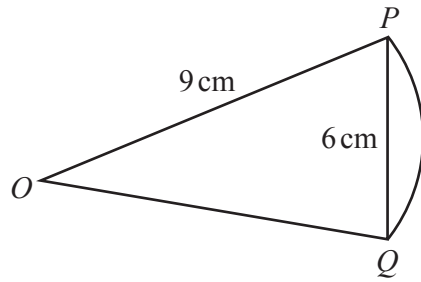
Find the number of sides of this regular polygon.

.... [3]

13

The diagram shows the speed–time graph for part of a car journey.

Calculate the total distance travelled during the 10 seconds.

.... m [2]

14

The diagram shows a sector of a circle with centre O and radius $9\,cm$.
The length of the chord PQ is $6\,cm$.

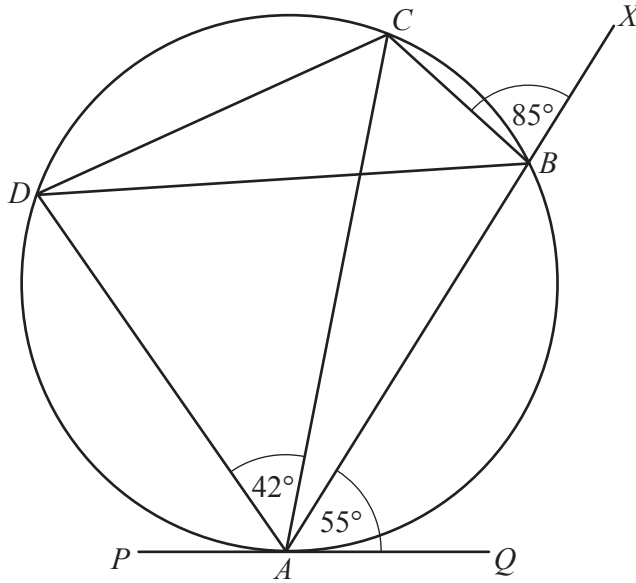Calculate the length of the arc PQ.

.... cm [3]

15 Simplify $\left(3125w^{3125}\right)^{\frac{1}{5}}$.

.... [2]

16 y is inversely proportional to x^2.
When $x = 3$, $y = 2$.

Find y when $x = 2$.

$y =$ .... [3]

17

NOT TO SCALE

ABCD is a cyclic quadrilateral, *ABX* is a straight line and *PQ* is a tangent to the circle at *A*.
Angle *CBX* = 85°, angle *BAQ* = 55° and angle *CAD* = 42°.

Find

(a) angle *CBD*

Angle *CBD* = ... [1]

(b) angle *ACB*

Angle *ACB* = ... [1]

(c) angle *ADC*

Angle *ADC* = ... [1]

(d) angle *BCD*

Angle *BCD* = ... [2]

(e) angle *PAD*.

Angle *PAD* = ... [1]

18 Two solids are mathematically similar and have volumes $81\,\text{cm}^3$ and $24\,\text{cm}^3$.
The surface area of the smaller solid is $44\,\text{cm}^2$.

Calculate the surface area of the larger solid.

.... cm^2 [3]

19 Find the values of x when $6x + y = 10$ and $y = x^2 - 3x + 10$.

$x =$ .... or $x =$ .... [3]

20 Find the *n*th term of each sequence.

(a)   −1,   0,   7,   26,   63,   …

.... [2]

(b)   24,   12,   6,   3,   1.5,   …

.... [2]

21 A car travels 14 km, correct to the nearest kilometre.
This takes 12 minutes, correct to the nearest minute.

Calculate the lower bound of the speed of the car.
Give your answer in kilometres per minute.

.... km/min [3]

22
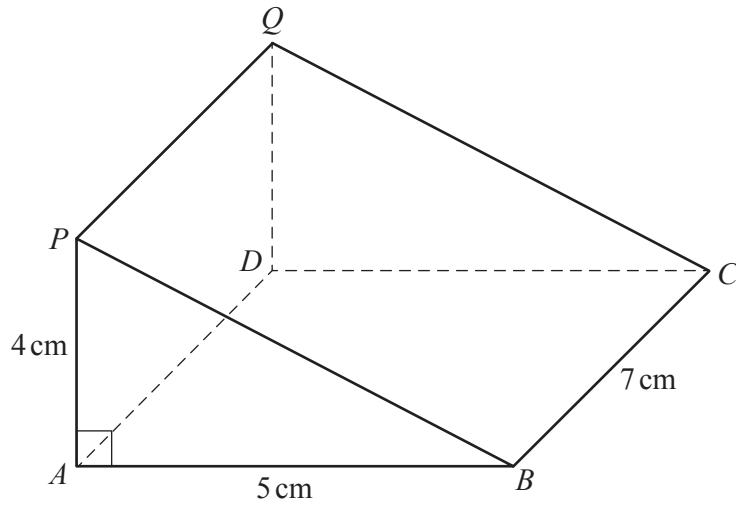
NOT TO SCALE

The diagram shows a triangular prism *ABCDQP* of length 7 cm.
The cross-section is triangle *PAB* with *PA* = 4 cm, *AB* = 5 cm and angle *PAB* = 90°.

Calculate the angle between the line *PC* and the base *ABCD*.

.... [4]

23 Simplify.

$$\frac{5x^2 - 19x + 12}{x^2 - 9}$$

.... [4]

24 The probability of Jamie hitting a target is $\frac{1}{3}$.

The probability that he hits the target for the first time on his nth attempt is $\frac{64}{2187}$.

Find the value of n.

$n = $ .... [2]

Question 25 is printed on the next page.

25 $\qquad$ $f(x) = x^3 + 1$

Find $f^{-1}(x)$.

$$f^{-1}(x) = \text{...} \quad [2]$$